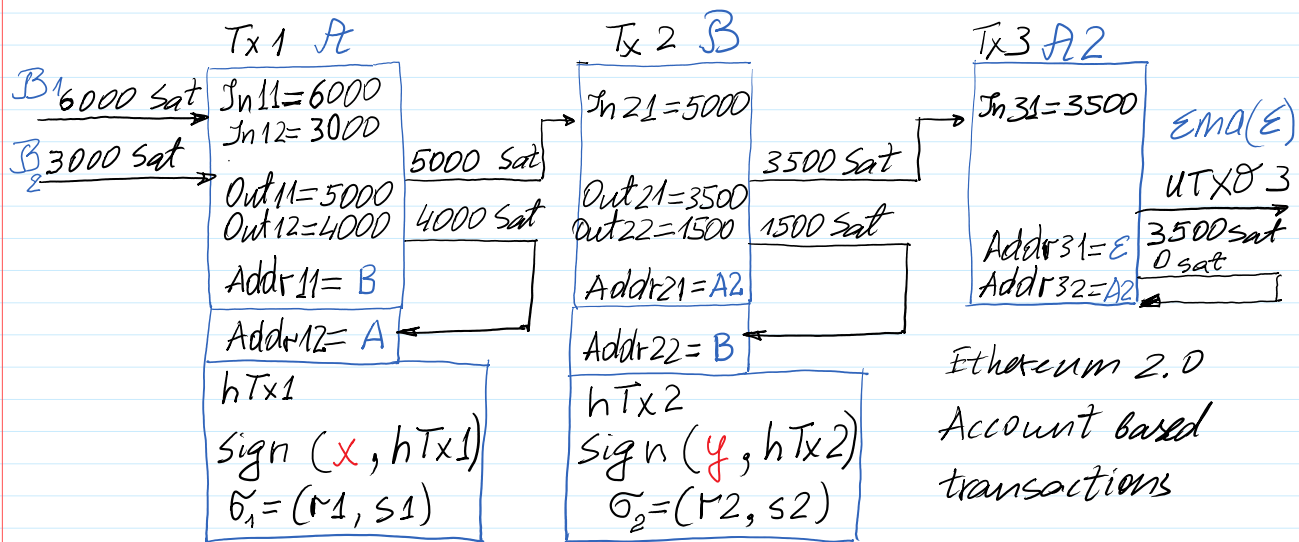


Block structure - Unspent Transaction Output (UTxO) model



$Tx1 = '1 : In11 = 6000 || In12 = 3000 || Out11 = 5000 || Out12 = 4000 || Rec1 = B || Rec2 = A'$
 $Tx2 = '2 : In21 = 5000 || Out21 = 3500 || Out22 = 1500 || Rec1 = A2 || Rec2 = B'$
 $Tx3 = '3 : In31 = 3500 || Out31 = 3500 || Out32 = 0 || Rec1 = E || Rec2 = A2'$

Transaction template:

$Tx_N = 'Tx_N : In11 = ... || In12 = ... || Out11 = ... || Out12 = ... || Rec1 = ... || Rec2 = ...'$

Transactions:

$Tx_1 = 'Tx_1 : In11 = 6000 || In12 = 3000 || Out11 = 5000 || Out12 = 4000 || Rec1 = B || Rec2 = A'$

$Tx_2 = 'Tx_2 : In21 = 5000 || Out21 = 3500 || Out22 = 1500 || Rec1 = A2 || Rec2 = B'$

$Tx_3 = 'Tx_3 : In31 = 3500 || Out31 = 3500 || Out32 = 0 || Rec1 = E || Rec2 = A2'$

$>> hTx_1 = h28('Tx_1 : In11 = 6000 || In12 = 3000 || Out11 = 5000 || Out12 = 4000 || Rec1 = B || Rec2 = A')$

$>> hTx_1 = h28(Tx_1)$

$hTx_1 = 996BB7C$

$>> hTx_2 = h28('Tx_2 : In21 = 5000 || Out21 = 3500 || Out22 = 1500 || Rec1 = A2 || Rec2 = B')$

$>> hTx_2 = h28(Tx_2)$

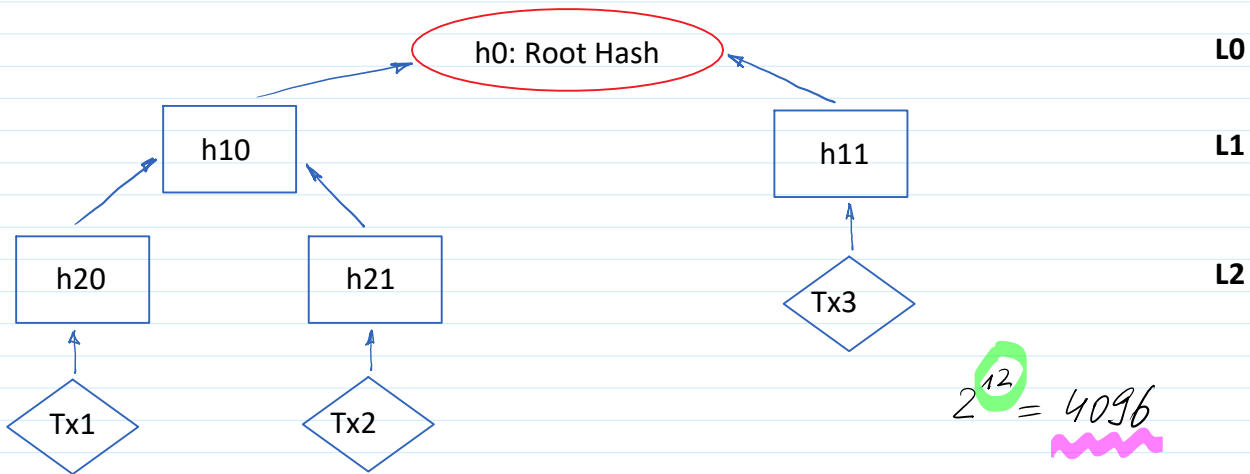
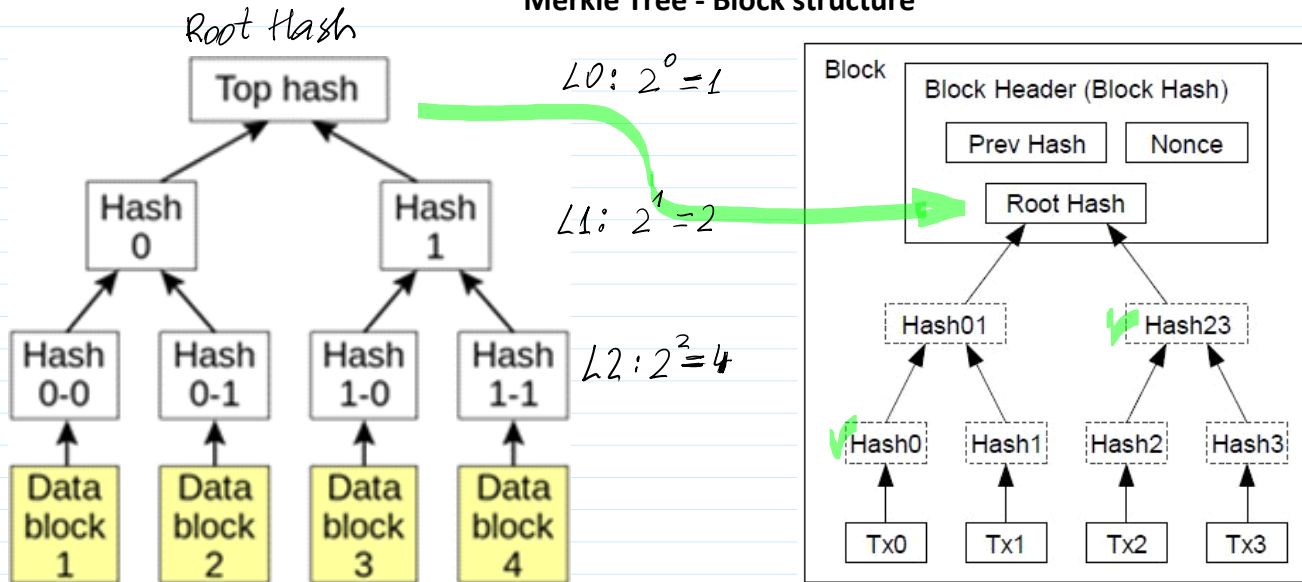
$hTx_2 = 977D75B$

$>> hTx_3 = h28('Tx_3 : In31 = 3500 || Out31 = 3500 || Out32 = 0 || Rec1 = E || Rec2 = A2')$

$>> hTx_3 = h28(Tx_3)$

$hTx_3 = 9201218$

Merkle Tree - Block structure



```
>> h20=h28(hTx_1)
```

```
h20 = 996BB7C
```

```
>> h21=h28(hTx_2)
```

```
h21 = 977D75B
```

```
>> h11=h28(hTx_3)
```

```
h11 = 9201218
```

```
>> h10=h28('996BB7C|977D75B')
```

```
h10 = 77F058A
```

Root Hash: h0

```
>> h0=h28('77F058A|9201218')
```

```
h0 = 91EFFF6
```

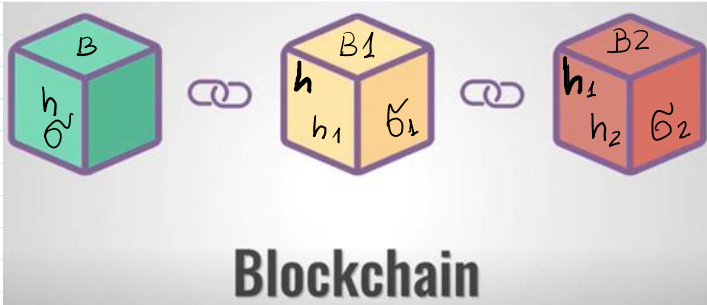
91EFFF6

Python : sha256

h20: 5B5412B

h21: D5C895A

h11: FEC59B7



Magic Number (4)		Block Size (4)	
Version (4)		Previous Block Hash (32)	
		sha 256 bits	
		Merkle Root(32)	
		Timestamp (4)	
Difficulty Target (4)		Nonce (4)	
Transaction Counter (Variable : 1-9)			
Transaction List (Variable : Upto 1 MB)			

BLOCK HEADER

Block size = 4 Bytes
 4 Bytes $\times$ 8 bits = 32 bits
 Block have
 $2^{32} - 1 = 4\,294\,967\,295$
 In ASCII encoding
 8 bits represents
 1 symbol a, b, c, ...
 Block represents
 536 870 912 symbols

Difficulty Target (DT): defines the complexity of block mining.
 In our simulation DT we will choose to find h-value of mining (mined block) having only 1 leading hexadecimal digit equal to 0.

$$h_{28}(\text{'RootHash_PrevHash_737327631'}) = h_{28()}$$

```

>> sha256('RootHash PrevHash 737327631')
ans = F4AE534CD226FAF799 8C8424B348E020BA80639A687E93A0B8C5130ED C51E6DE
                                     C51E6DE

>> sha256('RootHash PrevHash 737327632')
ans = B856211DF2EE15E30AB770C1A43CE014ECFE573182AFD885B28D96854DBC5F21

>> sha256('RootHash PrevHash 737327633')
ans = 9C18C764E347A58E57AC3F7A3C2874D5889A0E802699FEA47EEFF8C03BFEDA69

>> sha256('RootHash PrevHash 737327648')
ans = 01F9832B2431AFF9D2219E446D613B8361B9903B4B02B8A63990C6B2209785A6
  
```

After 17 trials with sequentially increasing nonce Malaga mined a block with DT=1 H-most-significant digit

48-31=17.

```
>> h28('RootHash PrevHash 737327631')
```

ans = C51E6DE

17 trials again.

```
>> h28('RootHash PrevHash 737327648')
```

ans = 09785A6

DT: to mine a block it is needed to find h-value having leading zero in hexadecimal format: C51E6DE

0XXXXXX

6 × 4 = 24 bits

F
1111

h-value is computed >> h28() → 7 hex numbers

What probability to mine a block? Number of 4 bits has $2^4 = 16$ values

0000	0001	0010	0011	...	1001	1010	1011	1100	1101	1110	1111
0	1	2	3		9	10	11	12	13	14	15
					A	B	C	D	E	F	

The number of possible h-values of 28 bits: 2^{28}

>> 2^{28} ans = 268 435 456

The number of adequate h-values: 2^{24}

>> $\text{int64}(2^{24})$ ans = 167 77 216

$$\Pr\{\text{to Mine}\} = \frac{2^{24}}{2^{28}} = \frac{1}{2^4} = \frac{1}{16}$$

DT: two leading hex number = 00

The number of adequate h-values: 2^{20}

00XXXXX

5 × 4 = 20

$$\Pr\{\text{to Mine}\} = \frac{2^{20}}{2^{28}} = \frac{1}{2^8} = \frac{1}{256}$$

DT: three leading hex number = 000

000XXXX

4 × 4 = 16

$$\Pr\{\text{to Mine}\} = \frac{2^{16}}{2^{28}} = \frac{1}{2^{12}} = \frac{1}{4096}$$

>> 2^{12} ans = 4096

$$\Pr\{\text{to Mine}\} = \frac{1}{2^{28}} = \frac{1}{268\,435\,456}$$

>> 2^{28} ans = 268 435 456

The probability to mine a block, e.g. in Bitcoin when

1 Eth = 10^{18} Wei

DT: is to find SHA256 value having 18 leading zeroes

```
>> sha256('RootHash PrevHash 737327631')
```

ans = F4AE534CD226FAF799 8C8424B348E020BA80639A687E93A0B8C5130EDC51E6DE

The number of possible h-values having 256 bits is 2^{256} .

The number of adequate h-values of SHA 256 is

$256 - 18 \cdot 4 = 256 - 72 = 184$ bits, that are represented 46 hex. num.

The number of adequate values is 2^{184} .

$$\text{Prob}\{\text{to mine}\} = \frac{2^{184}}{2^{256}} = 2^{184-256} = 2^{-72}$$

$$1 \text{ K} = 2^{10} = 1024$$

$$1 \text{ M} = 2^{20} = \dots$$

$$1 \text{ G} = 2^{30} = \dots$$

$$1 \text{ T} = 2^{40} = \dots$$

$$2^{72} \sim 4 \text{ GT} = 4 \cdot 2^{30} \cdot 2^{40} = 2^2 \cdot 2^{30} \cdot 2^{40} = 2^{72}$$

$$N = 4\,722\,366\,482\,869\,645\,213\,696$$

$$\text{Number of trials } N = 1 \text{ T} \cdot 1 \text{ G} \cdot 2^2 = 4 \cdot 2^{40} \cdot 2^{30}$$

Total net capacity $\text{Cap} \sim 2000 \text{ Th /sek}$

$$\text{Time } T = \frac{N}{\text{Cap}} = \frac{4 \cdot 2^{40} \cdot 2^{30}}{2000 \cdot 2^{40}} \approx \frac{4 \cdot 2^{30}}{2^{11}} = 4 \cdot 2^{19} \text{ s}$$

```
>> T=int64(4*2^19)
```

```
T = 2097152
```

```
>> Tval=T/3600
```

```
Tval = 583
```

```
>> Tdien=Tval/24
```

```
Tdien = 24
```

Private blockchain $\longleftrightarrow$ Public blockchain

Monero blockchain: Transactions sums $\rightarrow$ confidential $\rightarrow$ verifiable
 Sender }
 Receiver } $\rightarrow$ anonymous

How to realize confidential & verifiable transactions.